

Lesson 05

Image moments, LBP, HoG

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Statistical description of textures

LBP

HoG

Haar and Face Detection



First order statistics

- ▶ use the histogram of the image - namely the relative histogram

$$P(I) = \frac{\text{pixels with intensity } I}{\text{total pixels in region}} \quad (1)$$

- ▶ image moments

$$m_i = E[I^i] = \sum_{I=0}^{N_g-1} I^i P(I) \quad (2)$$

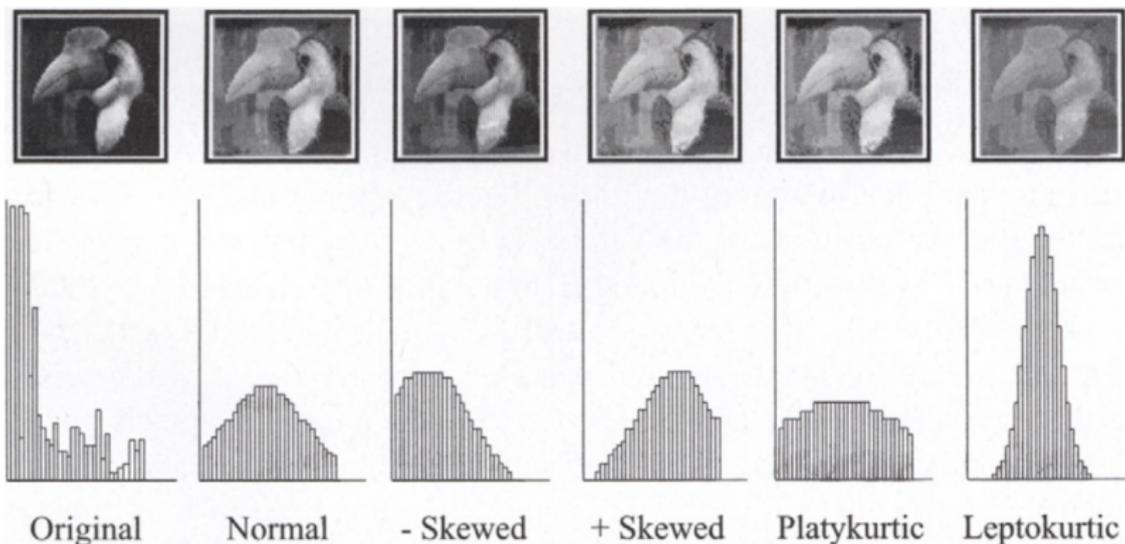
- ▶ image central moments

$$\mu_i = E[(I - E[I])^i] = \sum_{I=0}^{N_g-1} (I - m_1)^i P(I) \quad (3)$$

- ▶ entropy

$$H = -E[\log_2 P(I)] = - \sum_{I=0}^{N_g-1} P(I) \log_2 P(I) \quad (4)$$

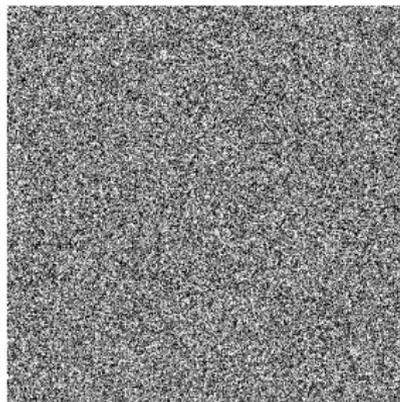




	Orig	Norm	-Skew	+Skew	Plat	Lept
μ_3	587	0	-169	169	0	0
μ_4	16609	7365	7450	7450	9774	1007
H	4.61	4.89	4.81	4.81	4.96	4.12

Second order statistics

- ▶ the second order statistics consider the structure of the data



- ▶ the images above have the same histogram, hence the same first order statistics

- ▶ **adjacency matrix** - for a given direction θ and distance d tells me how many times are two intensities in relation

$$\begin{aligned} 0^\circ : P(I(m, n) = I_1, I(m \pm d, n) = I_2) &= \\ &= \frac{\text{number of pairs with intensities } I_1, I_2}{\text{total number of possible pairs}} \end{aligned} \quad (5)$$

- ▶ θ is discretized into $\{0, 45, 90, 135\}$
- ▶ simpler form of the adjacency matrix is independent on θ and d
- ▶ in such case $P(i, j)$ tells us how many times pixels with intensity i are neighbors with pixels with intensity j (in the terms of probability)



- ▶ **Angular Second Moment** - the level of smoothness

$$ASM = \sum_{i=0}^{N_g-1} \sum_{j=0}^{N_g-1} P(i,j)^2 \quad (6)$$

- ▶ **Contrast** - big values for large contrast

$$CON = \sum_{i=0}^{N_g-1} \sum_{j=0}^{N_g-1} |i-j|^2 \log_2 P(i,j) \quad (7)$$

- ▶ **Homogeneity** - big values for small contrast

$$HOM = \sum_{i=0}^{N_g-1} \sum_{j=0}^{N_g-1} \frac{P(i,j)}{1 + |i-j|^2} \quad (8)$$

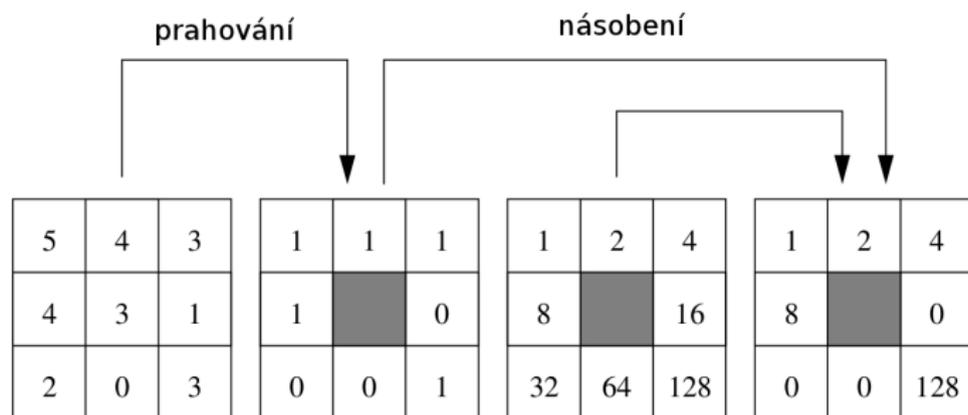
- ▶ **Entropy** - big values for small contrast

$$H_{xy} = - \sum_{i=0}^{N_g-1} \sum_{j=0}^{N_g-1} P(i,j) \log_2 P(i,j) \quad (9)$$



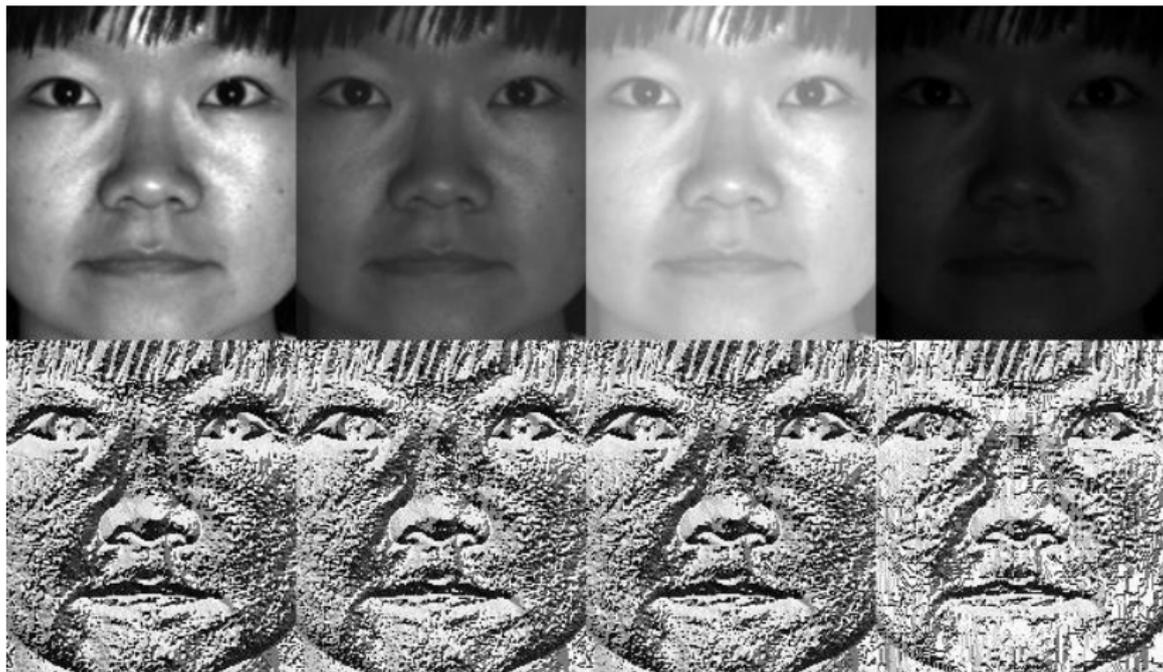
Local Binary Patterns

- ▶ Ojala 1996: How to describe texture around a pixel with one scalar?
- ▶ the basic version uses the 8-neighborhood of a pixel
- ▶ from this neighborhood a binary representation is build



$$\text{LBP} = 1+2+4+8+128 = 143$$

- ▶ for a given image patch a histogram of LBP codes is constructed and used as a feature



Classification of LBP codes

- ▶ **Classification with non-parametric test** - the difference between an unknown sample and a model is computed (Kullback–Leibler divergence)

$$KL(S, M) = \sum_{b=1}^B S_b \log \frac{S_b}{M_b} \quad (10)$$

- ▶ and since S_b is constant we can simplify to

$$L(S, M) = - \sum_{b=1}^B S_b \log M_b \quad (11)$$

- ▶ which is cross entropy



Classification of LBP codes

- ▶ if low number of samples is available we can use equation:

$$\chi^2 = \sum_{b=1}^B S_b \frac{(S_b - M_b)^2}{S_b + M_b} \quad (12)$$

- ▶ or if we need computational efficiency

$$H(S, M) = \sum_{b=1}^B \min(S_b, M_b) \quad (13)$$



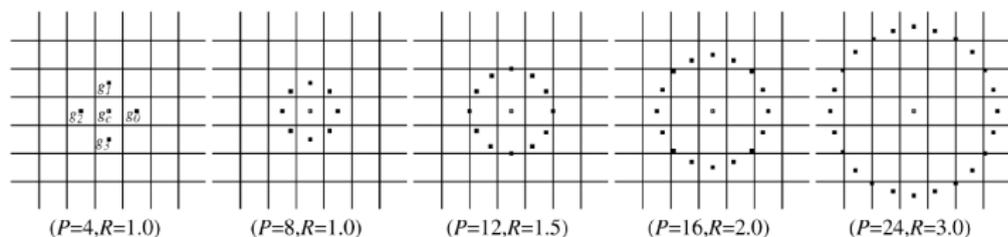
Extensions of LBP

- ▶ the basic LBP is invariant to brightness and contrast changes
- ▶ they are variant with scale and rotation - this is an issue
- ▶ texture definition:

$$T = t(g_c, g_0, \dots, g_{P-1}) \quad (14)$$

- ▶ the position of pixels in the neighborhood is defined as:

$$g_p = (-R \sin(2\pi p/P), R \cos(2\pi p/P)) \quad (15)$$



$$LBP_{P,R} = \sum_{p=0}^{P-1} s(g_p - g_c) 2^p \quad (16)$$

Rotation invariance and uniformity

- ▶ is achieved by rotating the local neighborhood

$$LBP_{P,R}^{ri} = \min (ROR(LBP_{P,R}, i) | i = 0, 1, \dots, P - 1) \quad (17)$$

- ▶ *ROR* is a bitwise rotation operator
- ▶ **uniform patterns** - are patterns with at most 2 changes between 0 and 1
- ▶ there are a total of 58 uniform patterns, while the rest are put into 59th bin
- ▶ Multi-resolution analysis - is used to cope with the resolution (scale) of the image

$$L_N = \sum_{n=1}^N L(S^n, M^n) \quad (18)$$

- ▶ with different *P* and *R* for each *n*



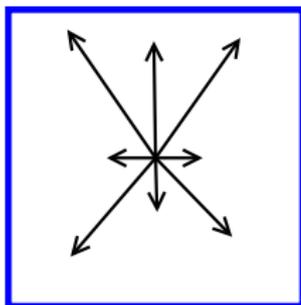
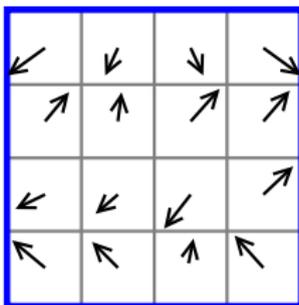
Histogram of Oriented Gradients

- ▶ method for describing images via histogram analysis
- ▶ the results of the method are directly dependent on the gradient operator, many had been tested
- ▶ the best results were obtained for simple gradient approximation

$$\begin{aligned} I_x &= I * [-1, 0, 1] \\ I_y &= I * [-1, 0, 1]^T \end{aligned} \quad (19)$$

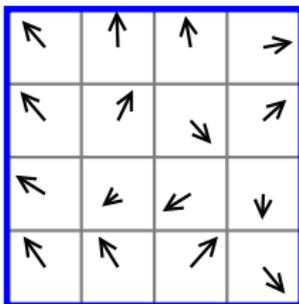
- ▶ for every pixel the size and orientation of the gradient is computed
- ▶ a histogram is constructed from these values
- ▶ the histogram is parametrized by interval i and number of sectors s
- ▶ the interval i is mostly $i = \langle 0, \pi \rangle, i = \langle 0, 2\pi \rangle$
- ▶ the magnitude of the histogram is added to each bin and moreover bilinearly distributed into neighboring bins





$$i = \langle 0, 2\pi \rangle$$

$$s = 8$$



$$i = \langle 0, \pi \rangle$$

$$s = 9$$

Histogram Normalization

- ▶ the normalization is useful to cope with brightness transformations
- ▶ the most used normalizations are

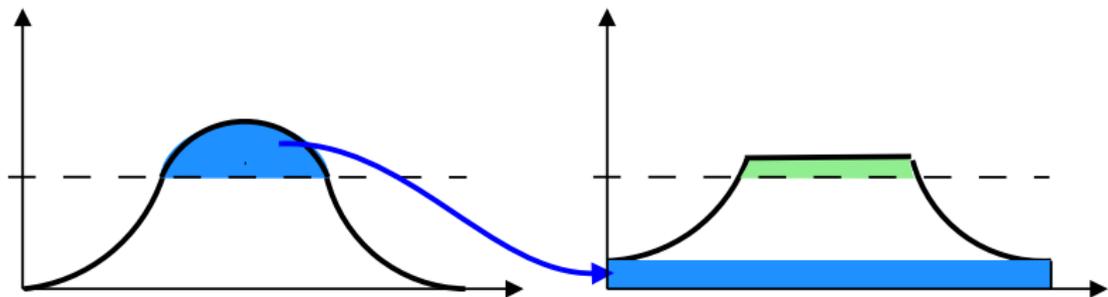
$$L^1 - norm = \frac{v}{(\|v\|_1 + e)}, \quad (20)$$

$$L^1 - sqrt = \sqrt{\frac{v}{(\|v\|_1 + e)}}, \quad (21)$$

$$L^2 - norm = \frac{v}{\sqrt{(\|v\|_2^2 + e^2)}}, \quad (22)$$

- ▶ v is the histogram to be normalized and e is a small constant
- ▶ a special case of normalization $L_2 - Hys$ - the normalized vector is clipped as in CLAHE

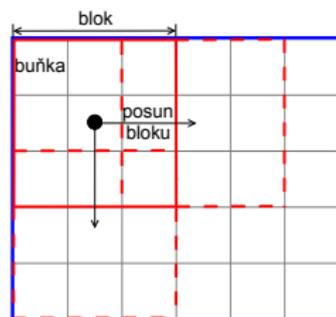




- ▶ the values (after normalization) above a given threshold are distributed into all the bins
- ▶ the process is repeated until no value is above the threshold

HoG descriptor

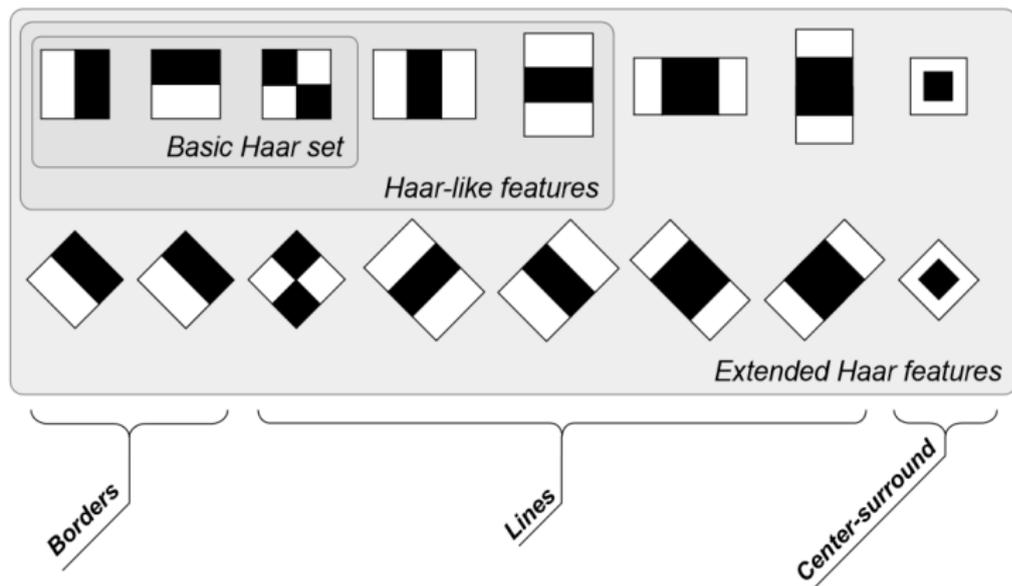
- ▶ the image is divided into blocks of size (k, k)
- ▶ individual blocks are divided into cells of size (l, l)



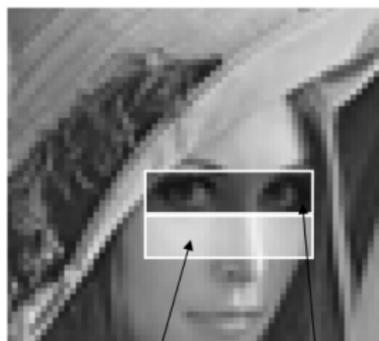
- ▶ for each cell the normalized histograms of gradients are computed
- ▶ for each block the cell histograms are averaged
- ▶ then the block shifts by some pixels and the process is repeated
- ▶ the averaged block histograms are concatenated to obtain the descriptor

Haar-like features

- ▶ Haar-like features are used for image transformation similar to cosine transform



- ▶ the Haar-like filters can be computed efficiently by using integral image
- ▶ the black regions are subtracted from the white regions



R_{white} R_{black}



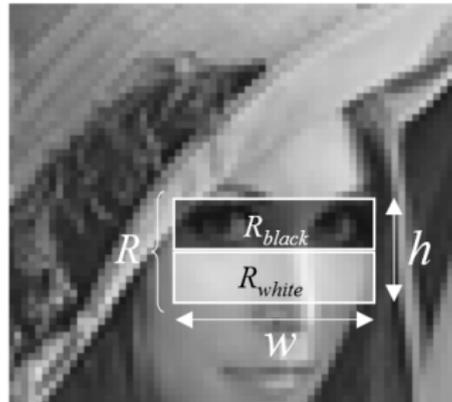
$$F_{Haar} = E(R_{white}) - E(R_{black})$$

Normalization (monotonic illumination changes)



$$F_{Haar} = \frac{E(R_{black}) - E(R_{white})}{\underbrace{\sqrt{|E(R_{\mu})^2 - E(R_{\mu}^2)|}}_{Standard\ Deviation}}$$

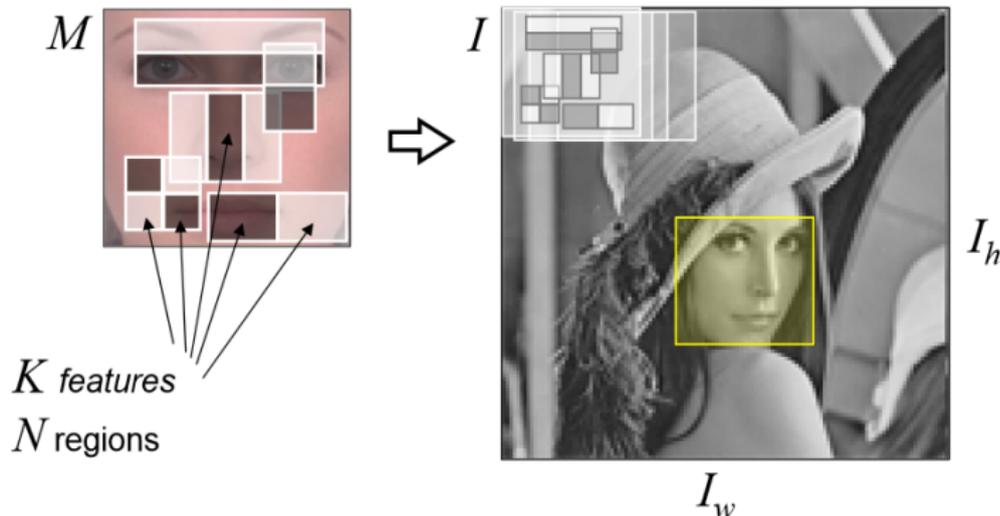
Normalization (monotonic illumination changes and scale)



$$F_{Haar} = \frac{E(R_{black}) - E(R_{white})}{w \cdot h \cdot \sqrt{|E(R_{\mu})^2 - E(R_{\mu}^2)|}}$$

Face detection

- ▶ a sliding window in different scales is used to compute responses on different Haar filters



- ▶ a boosted classifier is used to train the right responses to certain (most informative) filters